Model Quesiton − 3
Subject : Mathematics XII (Mat. 402/008)

Time: 3 hrs F.M. 75

Attempt all the questions:

Group "A"

Rewrite the correct option in your answer sheet:

11X1=11

1) What is the value of C (12, 9)?

a. 120 b. 220

c. 240

d. 260

2) The polar form of the complex number 2 + 2i is

\ 4 4	a.	$2\sqrt{2}$	$\left(\cos\frac{\pi}{4} + i \operatorname{s}\right)$	$ \sin \frac{\pi}{4} $
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$$b. \ 2\left(\cos\frac{\pi}{4} + i\sin\frac{\pi}{4}\right)$$

c.
$$4\left(\cos\frac{\pi}{4} + i\sin\frac{\pi}{4}\right)$$

d.
$$2\sqrt{2}\left(\sin\frac{\pi}{4} + i\cos\frac{\pi}{4}\right)$$

The value of $\cos\left(Arc\cos\frac{2}{3}\right)$ is 3)

a.
$$\frac{\pi}{4}$$

a.
$$\frac{\pi}{4}$$
 b. $\frac{4}{3}$ c. $\frac{2}{3}$

c.
$$\frac{2}{3}$$

d.
$$-\frac{4}{3}$$

The vertices of the ellipse $\frac{x^2}{4} + \frac{y^2}{9} = 1$ are 4)

d.
$$(0, \pm 3)$$

If $|\vec{a}| = \sqrt{14} |\vec{b}| = \sqrt{29}$ and $\vec{a} \cdot \vec{b} = 20$, then the value of $\vec{a} \times \vec{b}$ is

a.
$$\sqrt{6}$$

b.
$$2\sqrt{6}$$

What is the seventh term of $(2x+y)^{12}$? 6)

a. C (12,7)
$$2^6 x^6 y^6$$

c. C (12,6)
$$2^7 x^7 y^7$$

Given that $\sum xy = 92$, $\sum x^2 = 76$, $\sum y^2 = 186$ and n = 6. What is the correlation coefficient 7) between x and y?

What is the value of $x \to \frac{\pi}{2} \frac{\sec 3x}{\sec x}$? 8)

a.
$$\frac{1}{3}$$

a.
$$\frac{1}{3}$$
 b. $-\frac{1}{3}$

d. 2

The value of the integral $\int \frac{1}{a^2 + x^2} dx$ is

a.
$$\frac{1}{a} \tan^{-1} \frac{x}{a} + C$$

b.
$$\frac{1}{a}\cos^{-1}\frac{x}{a} + C$$

c.
$$\frac{1}{a}\sin^{-1}\frac{x}{a} + C$$

d.
$$\frac{1}{a}\sec^{-1}\frac{x}{a}+C$$

The highest point reached by a projectile is 20 m above the horizontal. If the initial velocity is 10) $20\sqrt{2}$ m/s, the angle of projection when g 10 m/s² is

a. 30⁰

b. 60⁰

c. 45⁰

d. 75⁰

A manufacturer sells a product at \$8 per unit, selling all that is produced. Fixed cost is \$ 5000 and variable cost per unit is $\frac{22}{9}$ dollars. What is the total revenue at the break even point?

- a. 5200
- b. 6000
- c. 7000
- d.7200

11) If the equation $x^2 - (3a - 1) \times 2(a^2 - 1) = 0$ has equal roots, then the value of a is

- a. 3
- b. 4
- c. -3
- d.-4

Group "B"

Short answer questions:

8X5=40

- 12) From 6 gentlemen and 4 ladies, a committee of 5 is to be formed. In how many ways can this be done so as to include at least one lady?
- 13) Let $G = Q \{1\}$, the set of all rational numbers without 1. Suppose an operation * defined on G is given by

$$a * b = a + b - ab$$

Show that the system is a group.

14) Find the coordinates of the vertices, eccentricity and foci of the curve:

$$9x^2 - 16y^2 - 18x - 64y - 199 = 0.$$

- 15) Verify Rolle's theorem for the function $f(x) = \sqrt{1 x^2}$ in the interval [-1, 1]
- 16) Evaluate: $\int \frac{dx}{2 + \cos x}$
- 17) Calculate the coefficient of correlation from the following:

Х	14	16	19	22	24	30
Υ	14	22	20	24	23	26

18) Solve the following system of equations using Gaussian elimination method:

$$2x_1 + 3x_3 = 7$$

$$3x_1 - 2x_2 + 2x_3 = 1$$

$$2x_1 + 3x_2 - 3x_3 = 5$$

19) A balloon is rising with an acceleration f. Prove that the fraction of the weight of the balloon which must be emptied out of the balloon in order to double the acceleration is $\frac{f}{g+2f}$

Group "C"

Long answer questions:

3X8=24

20)

a) Solve:
$$\sin x \frac{dy}{dx} + (\cos x)y = x \sin x$$

3

b) Find the derivative of x^{cosx}.

3

c) Show that:
$$\frac{2}{3!} + \frac{4}{5!} + \frac{6}{7!} + \dots = \frac{1}{e}$$

21)

a) Define vector product of two vectors. Interpret it geometically.

3

3

b) Use vector method to prove that:
$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

5

22)

a) Find the polar form of the complex number $-1 + \sqrt{3}i$

b) Solve:
$$2\frac{dy}{dx} = \frac{y}{x} + \frac{y^2}{x^2}$$

3

c) Sum to infinity:
$$1 + \frac{3}{4} + \frac{7}{16} + \frac{15}{64} + \dots$$

3

Answers:

Group A

1) (b)	2) (a)	3) (c)	4) (d)
5) (a)	6) (b)	7) (d)	8) (b)
9) (a)	10) (c) OR (d)	11) (a)	

Group B

14) Vertices = (5, -2) and (-3, -2)
$$e = \frac{5}{4}$$

Foci =
$$(6, -2)$$
 and $(-4, -2)$

$$16) \frac{2}{\sqrt{3}} \tan^{-1} \left(\frac{1}{\sqrt{3}} \tan \frac{x}{2} \right) + c$$

18)
$$x_1=1$$
, $x_2=2$, $x_3=1$

Group C

(a)
$$y \sin x = -x \cos x + \sin x + C$$

(b)
$$x^{\cos x} \left(\frac{\cos x}{x} - \sin x \log x \right)$$

(a)
$$2(\cos 150^{\circ} + i \sin 150^{\circ})$$

(h)	11	$-\left(1+\sqrt{3}i\right)$
(D)	$\frac{1}{\sqrt{2}}$	$(1 + \sqrt{3}i)$

(c)
$$\frac{8}{3}$$